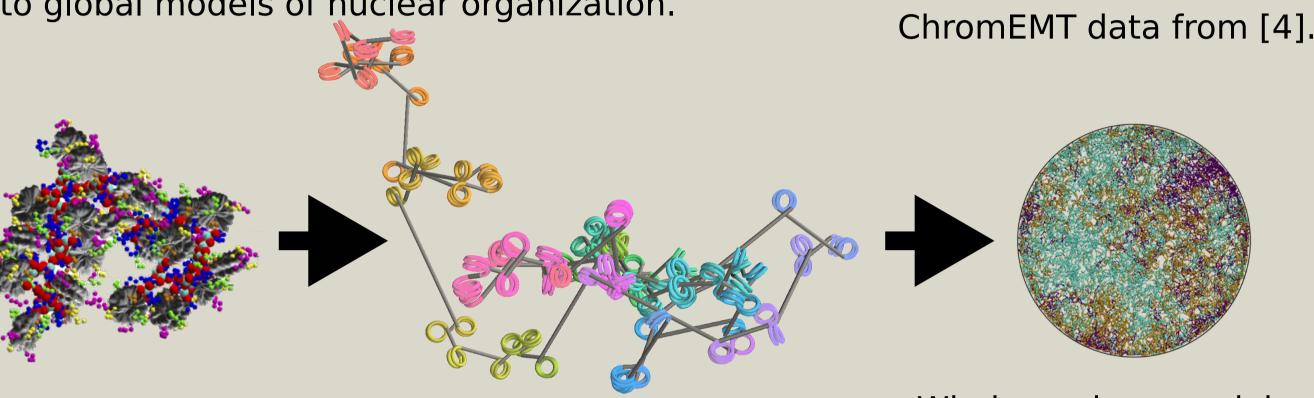
## Stanford University

# **Nucleosome Heterogeneity Governs Chromatin Elasticity**

#### Modeling Chromatin

- In vivo chromatin is extremely heterogeneous.
- Detailed models of chromatin often include nucleosome geometry and heterogeneity.
- However, it is difficult to isolate the effects of nucleosome localization in these complex models.
- Using a purely analytical approach, we can construct an intuitive picture for how nucleosome positioning affects chromatin structure.
- This allows us to incorporate nucleosome positioning into global models of nuclear organization.

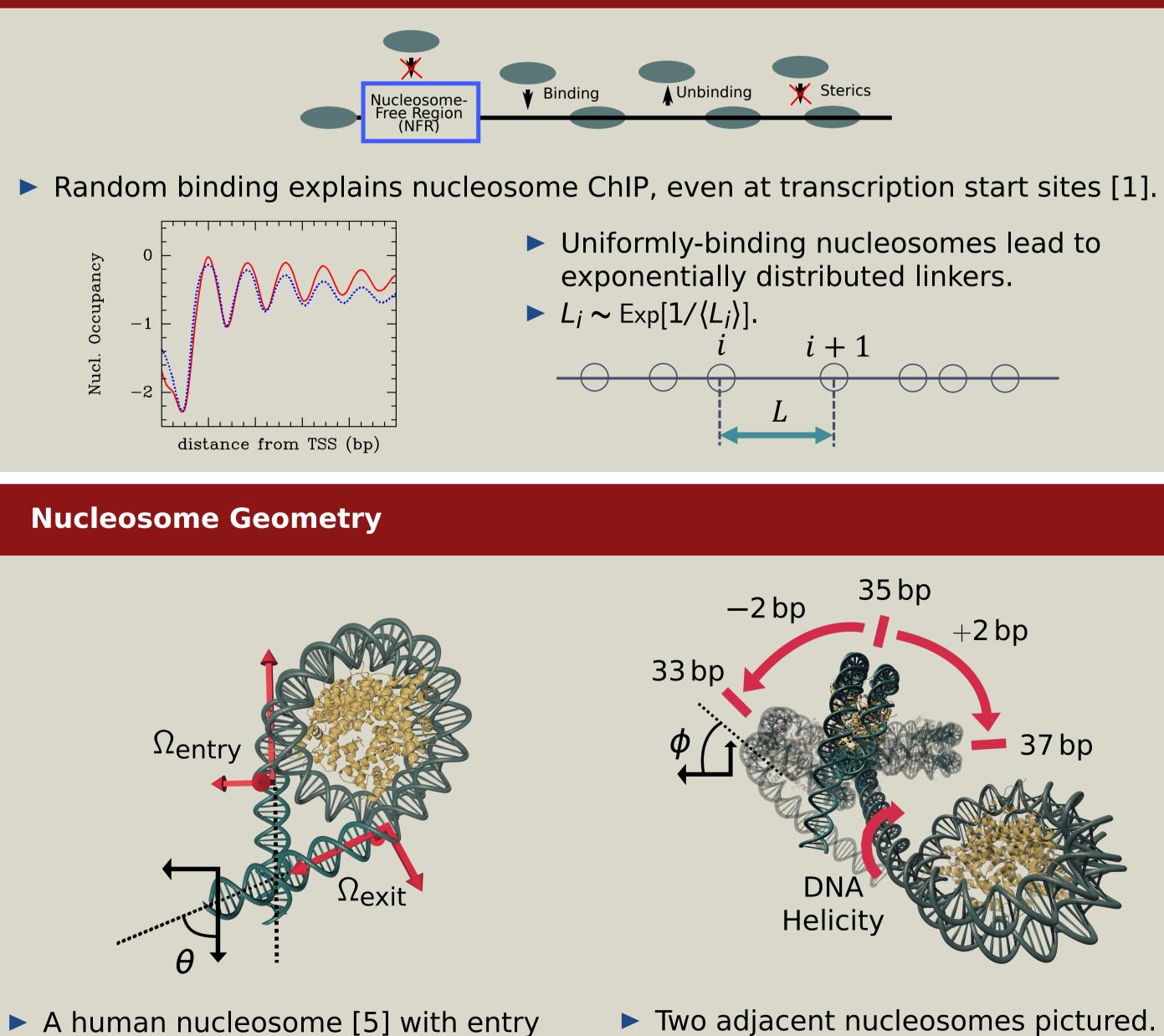


Detailed model [2].

Simplified model (this poster).

Whole-nucleus model (MacPherson et. al., in preparation).

**Realistic Nucleosome Positioning** 



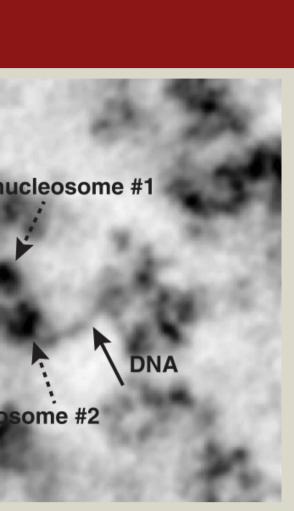
- A human nucleosome [5] with entry  $(\Omega_{entry})$  and exit  $(\Omega_{exit})$  orientations of the bound DNA labeled.
- The amount of DNA wrapping the nucleosome dictates the spherical angle  $\theta$ .

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by linker length.

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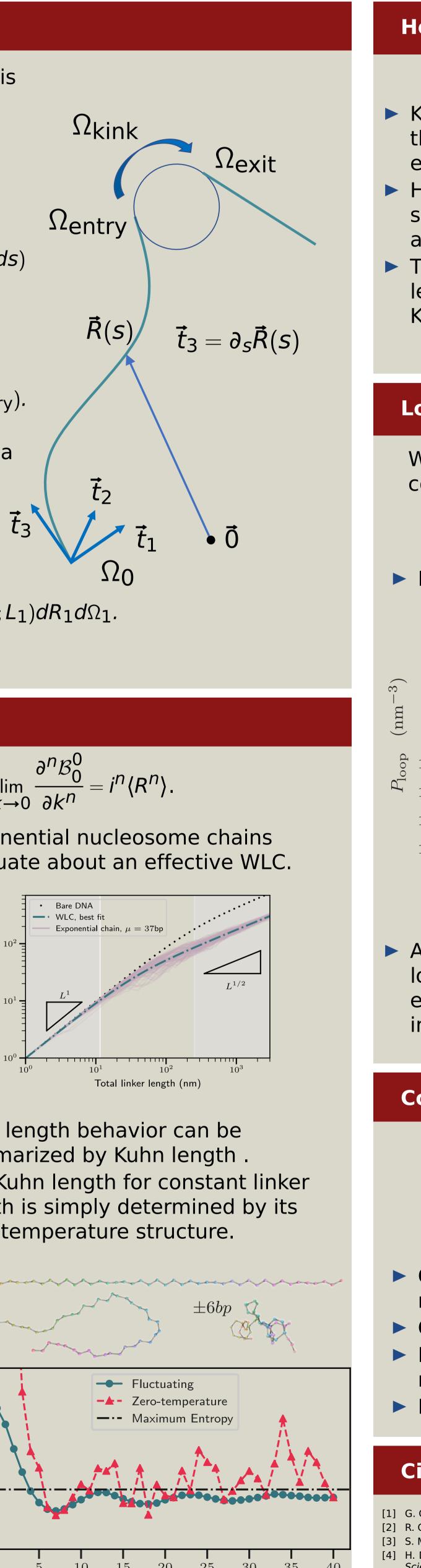
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The histone octamer must align with the major groove of the double helix.  $\blacktriangleright$  Therefore, the relative angle  $\phi$ between nucleosomes is determined

#### Kinked WLC

The energy of a twistable wormlike chain (tWLC) is
$eta \mathcal{E} = rac{l_p}{2} \int_0^L \omega_1^2 + \omega_2^2 ds + rac{l_t}{2} \int_0^L (\omega_3 -  au)^2 ds,$
where $\partial_s \vec{t}_i(s) = \vec{\omega}(s) \times \vec{t}_i(s)$ and $\tau = 10.5$ bp <sup>-1</sup> . Its Green's function
$G(\vec{R}, \Omega   \Omega_0; L) = \int_{\Omega(s=0)}^{\Omega(s=L)} \mathscr{D}[\Omega(s)] \exp[-\beta \mathcal{E}] \delta(\vec{R} - \int_0^L \vec{t}_3 ds)$
<ul> <li>has an exact solution in Wigner D-functions [3].</li> <li>We rotate the Green's function by Ω<sub>kink</sub> using</li> </ul>
$\mathcal{D}_{l}^{mj}(\Omega_{ ext{entry}}\cdot\Omega_{ ext{kink}}) = \sum_{k} \sqrt{rac{8\pi}{2l+1}} \mathcal{D}_{l}^{mk}(\Omega_{ ext{kink}}) \mathcal{D}_{l}^{kj}(\Omega_{ ext{entry}})$
• Concretely, we compute a matrix $\mathcal{B}$ representing a (linker, nucleosome) pair in Fourier space $\hat{G}(\vec{k}, \Omega   \Omega_0; L) = \sum \sum \mathcal{B}^{\mu}_{\mu_0} \mathcal{D}^{\mu}(\Omega) \mathcal{D}_{\mu_0}(\Omega_0).$
Linkers combine via convolution (multiplying $\mathcal{B}'$ s)
$G(\vec{R}, \Omega   \Omega_0; L_1, L_2) = \int G(\vec{R} - \vec{R_1}, \Omega   \Omega_1; L_2) G(\vec{R_1}, \Omega_1   \Omega_0; L_2)$
J
End-to-end Distance
We compute the end-to-end distance $\langle R^2 \rangle$ using $\lim_{\nu \to \infty} \frac{1}{\nu}$
Constant linker length chains will have Exponenties.
$\left(\begin{array}{c} \textbf{H}\\ H$
<ul> <li>Summa summa sum summa s</li></ul>
<ul> <li>As linker variability increases, the zero-temperature structure becomes a random walk.</li> <li>The "diffusivity" of this random walk determines the structure of heterogeneous chains.</li> <li>Very little linker length heterogeneity is need to create a random walk at zero temperature.</li> </ul>



Linker length variability  $\pm \sigma$  (bp)

### **Heterogeneous Chain Elasticity**

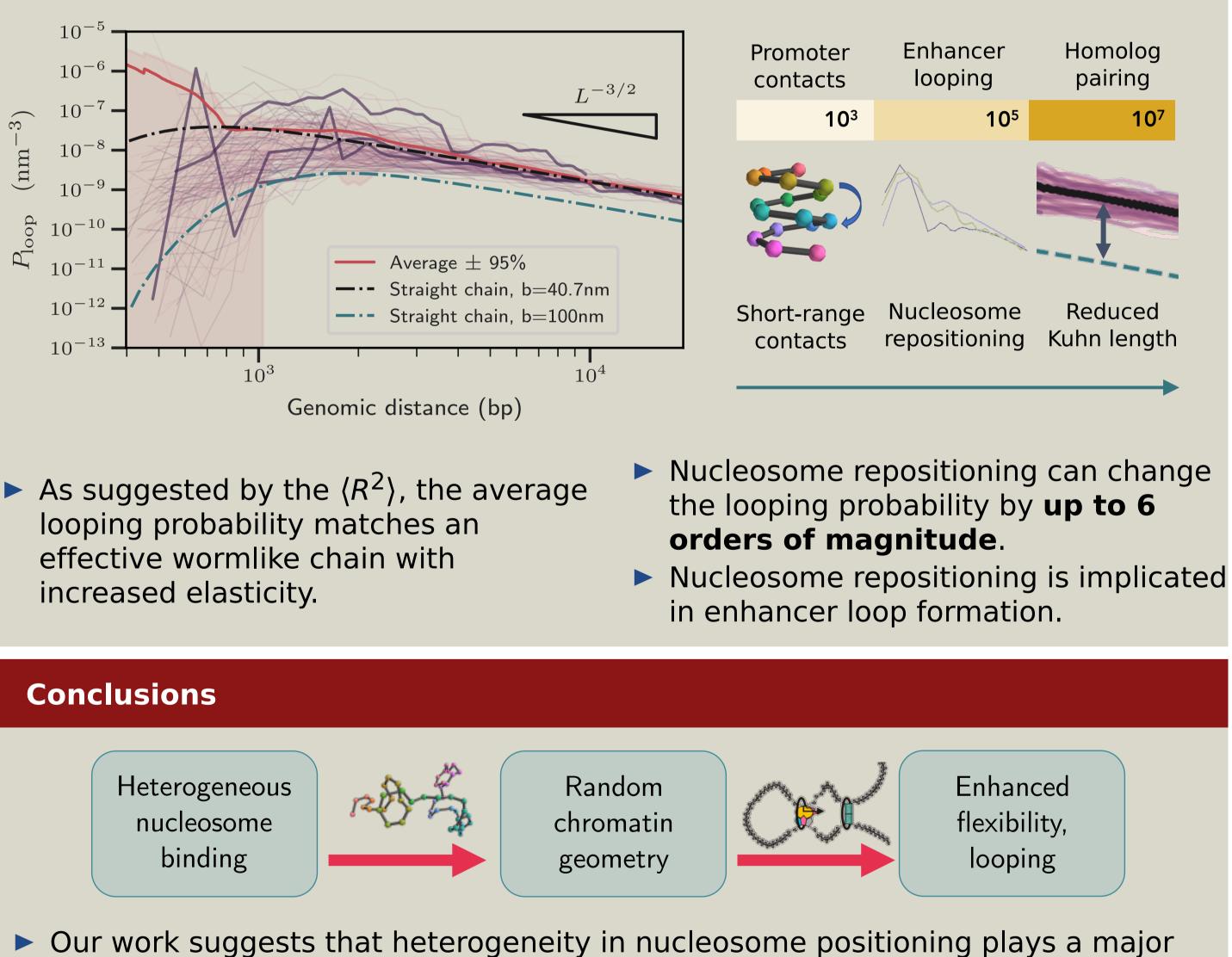
- Kuhn length depends only on the mean linker length for exponential chains.
- Heterogenous chains are less sensitive to changes in average nucleosome spacing.
- The chromatin chain's Kuhn length approaches bare WLC Kuhn length like ~  $1/\langle L_i \rangle$ .

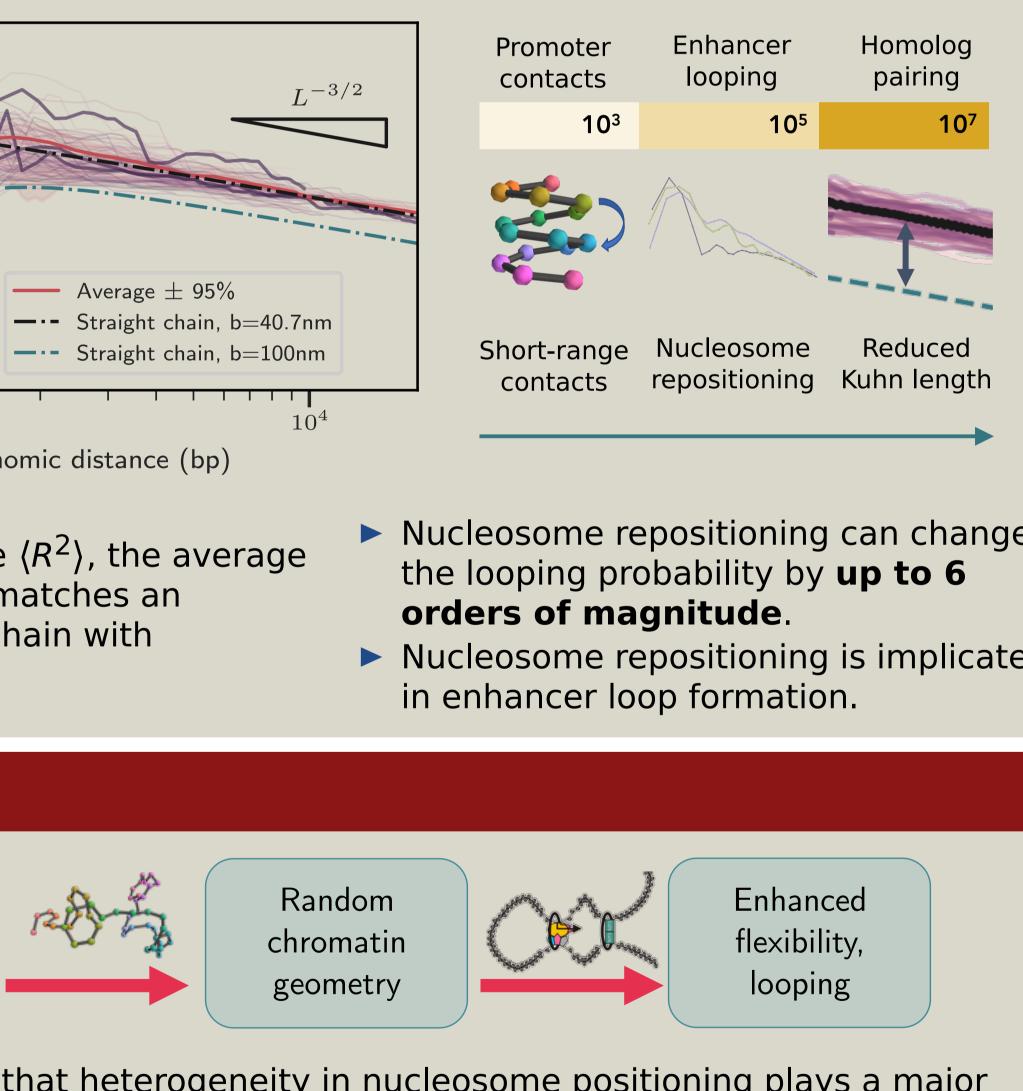
#### **Looping Probabilities**

We compute the looping probabilities as a modified J-factor, ignoring orientational contributions:

$$P_{\text{loop}}(L) = G(\vec{0}|L) = \frac{1}{2\pi^3} \int G(\vec{k}|L) \exp(-i\vec{k}\cdot\vec{R}) d\vec{k} \Big|_{\vec{R}=0} = \frac{1}{2\pi^2} \int k^2 j_0(0) \mathcal{B}_0^0(k;L) d\vec{k}.$$

For  $\langle L_i \rangle = 56$  bp:

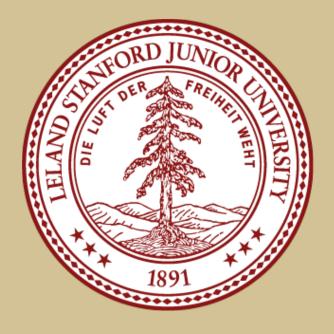


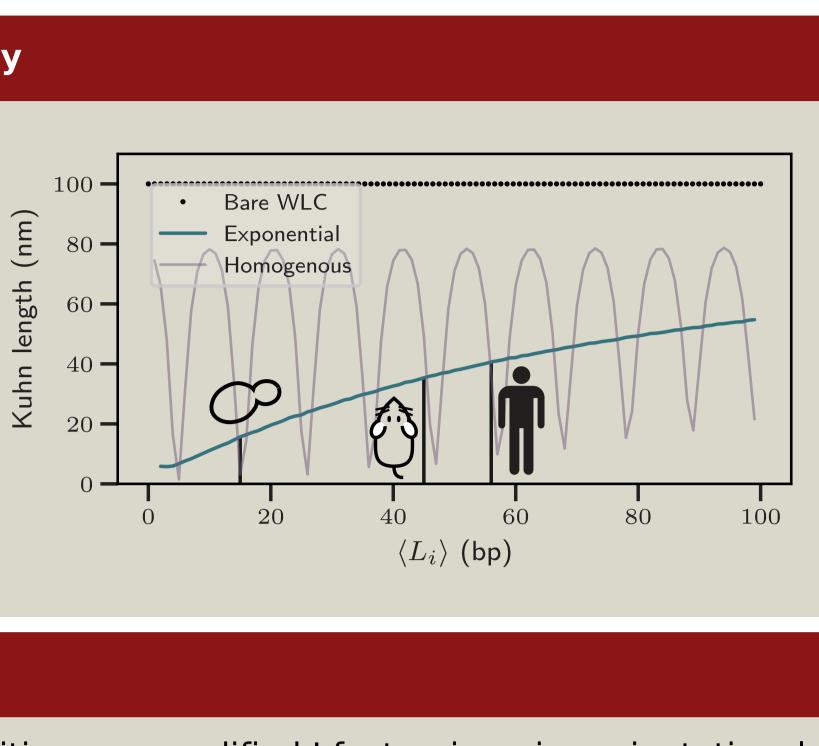


- role in the local and global behavior of chromosomal DNA.
- Chromatin is an effective WLC with reduced persistence length.
- modified WLC.

#### Citations

- Science, 357(6349):eaag0025, July 2017.
- nucleosome core particle with genetically-incorporated H4 tetra-acetylation. *Scientific Reports*, 5:17204, Nov. 2015.





Even one base pair of linker length variance can be sufficient to create this

Nucleosome repositioning can expedite looping out to tens of kilobases.

[1] G. Chevereau, L. Palmeira, C. Thermes, A. Arneodo, and C. Vaillant. Thermodynamics of Intragenic Nucleosome Ordering. *Physical Review Letters*, 103(18), Oct. 2009. [2] R. Collepardo-Guevara and T. Schlick. Chromatin fiber polymorphism triggered by variations of DNA linker lengths. PNAS, 111(22):8061–8066, June 2014. [3] S. Mehraeen, B. Sudhanshu, E. F. Koslover, and A. J. Spakowitz. End-to-end distribution for a wormlike chain in arbitrary dimensions. Physical Review E, 77(6), June 2008. [4] H. D. Ou, S. Phan, T. J. Deerinck, A. Thor, M. H. Ellisman, and C. C. O'Shea. ChromEMT: Visualizing 3D chromatin structure and compaction in interphase and mitotic cells.

[5] M. Wakamori, Y. Fujii, N. Suka, M. Shirouzu, K. Sakamoto, T. Umehara, and S. Yokoyama. Intra- and inter-nucleosomal interactions of the histone H4 tail revealed with a human